



# GeomGCL: Geometric Graph Contrastive Learning for Molecular Property Prediction

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<https://github.com/agave233/GeomGCL>

2022. 12. 22 • ChongQing

**2022\_AAAI**



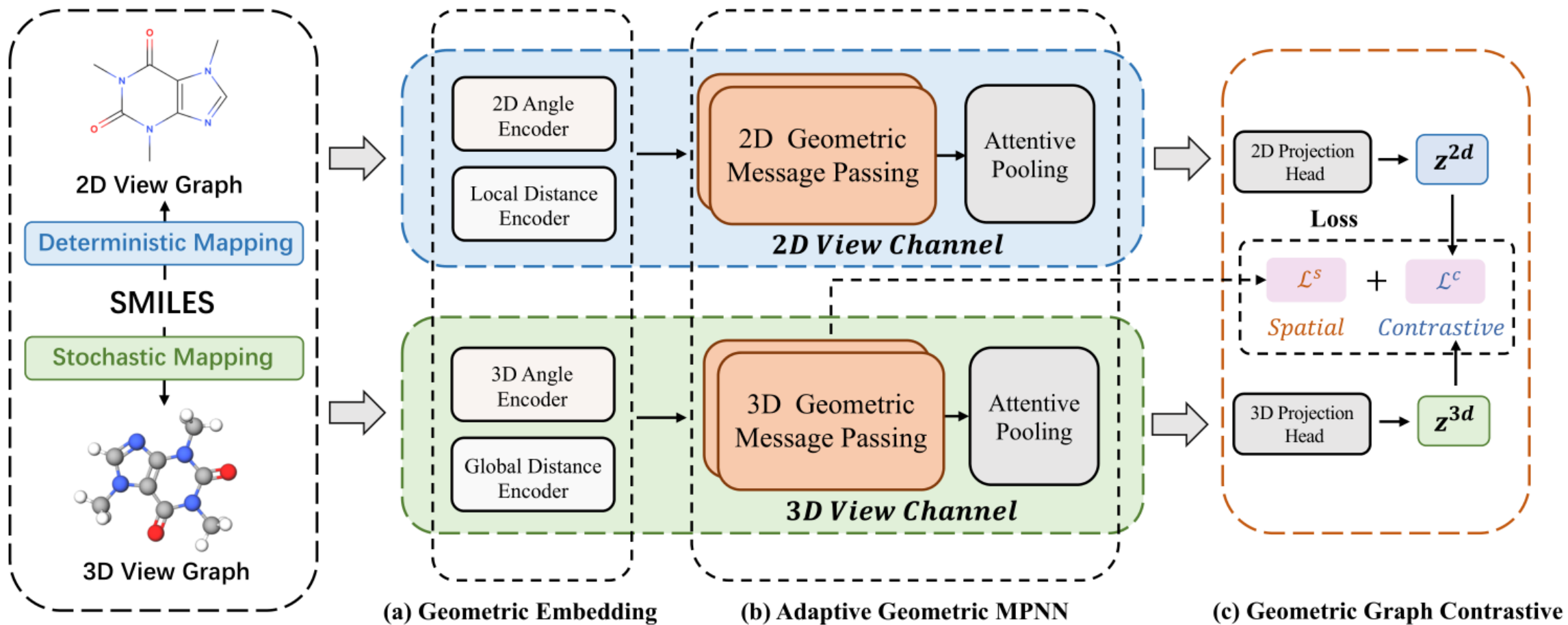
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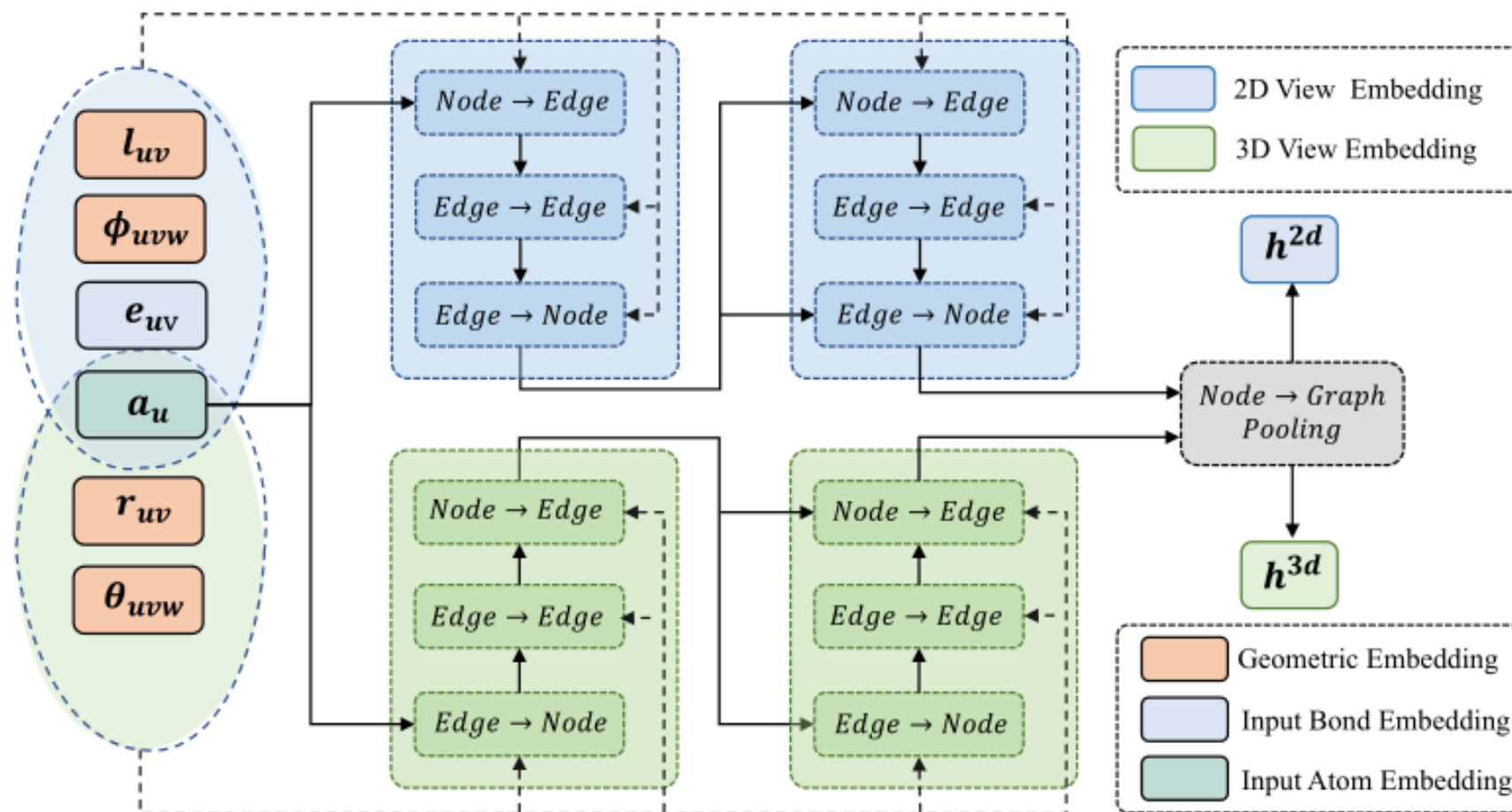
**Reported by JiaWei Cheng**



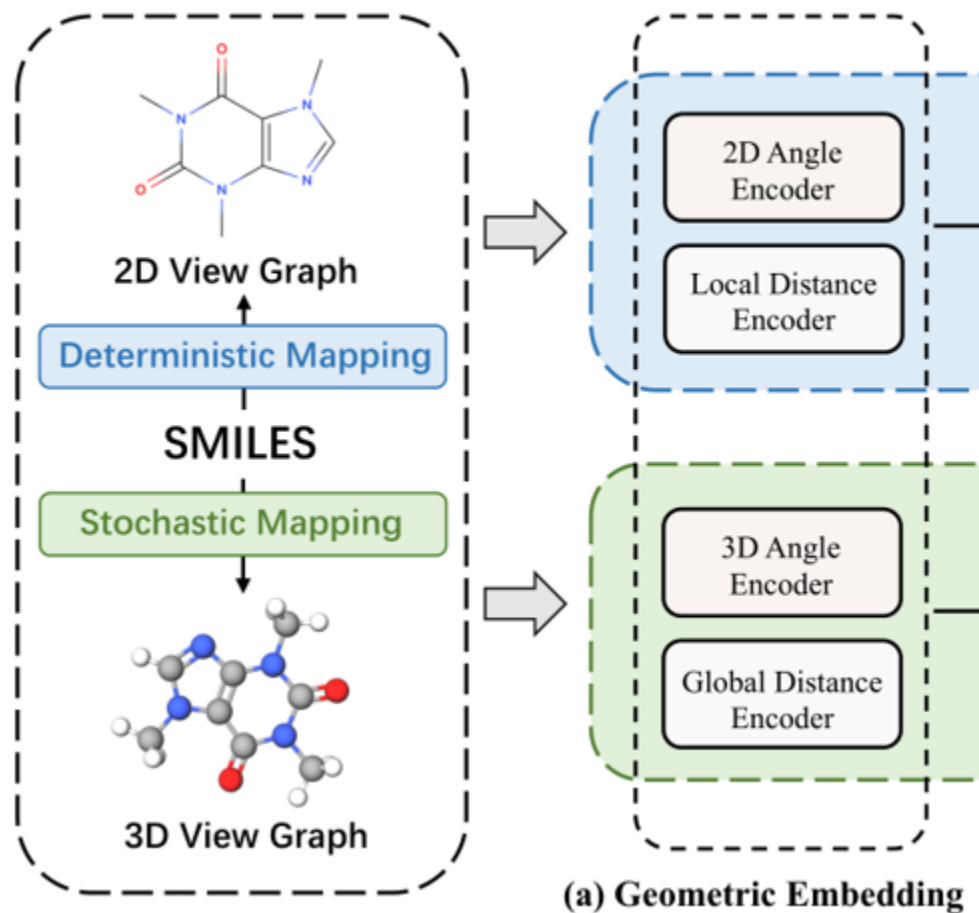
# Overview



# Overview



# Method



$$l = RBF(l) = \sum_{k=1}^K \exp(-\beta_l(\exp(-l) - \mu_{l,k})^2) \quad (1)$$

$$r = RBF(r) = \sum_{k=1}^K \exp(-\beta_r(\exp(-r) - \mu_{r,k})^2) \quad (2)$$

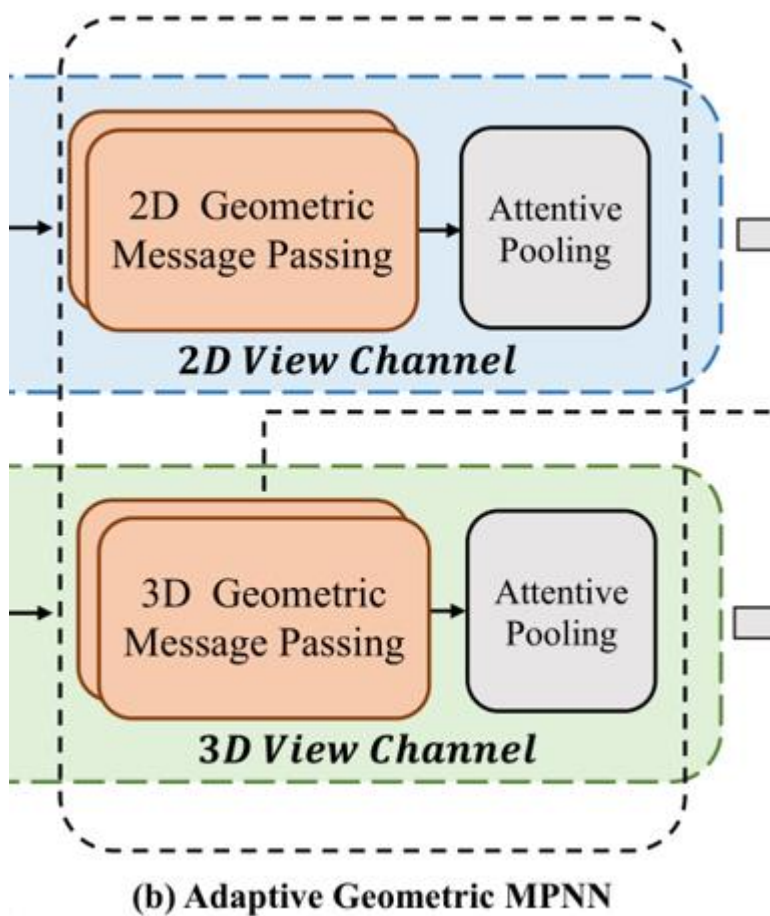
$$\phi = RBF(\phi) = \sum_{k=1}^K \exp(-\beta_\phi(\phi - \mu_{\phi,k})^2) \quad (3)$$

$$\theta = RBF(\theta) = \sum_{k=1}^K \exp(-\beta_\theta(\theta - \mu_{\theta,k})^2) \quad (4)$$

the  $K$  central points  $\{\mu_{*,k}\}$  are uniformly selected between  $\exp(-*)$  ( $*$  is  $l$  or  $d$ ) and 1, while  $\beta_* = (\frac{2}{K}(1 - \exp(-*)))^{-2}$ .

For 2D and 3D angles, each  $\mu_{*,k}$  is between 0 and  $\pi$  with  $\beta_* = (\frac{2\pi}{K})^{-2}$ , where  $*$  denotes  $\phi$  or  $\theta$ .

# Method



## Node $\rightarrow$ Edge Message Passing

$$e_{uv}^{2d,t} = MLP(\mathbf{a}_u^{2d,t-1} \parallel \mathbf{a}_v^{2d,t-1} \parallel \mathbf{e}_{uv}^0) \quad (5)$$

$$e_{uv}^{3d,t} = MLP(\mathbf{a}_u^{3d,t-1} \parallel \mathbf{a}_v^{3d,t-1} \parallel \mathbf{r}_{uv}) \quad (6)$$

## Edge $\rightarrow$ Edge Message Passing

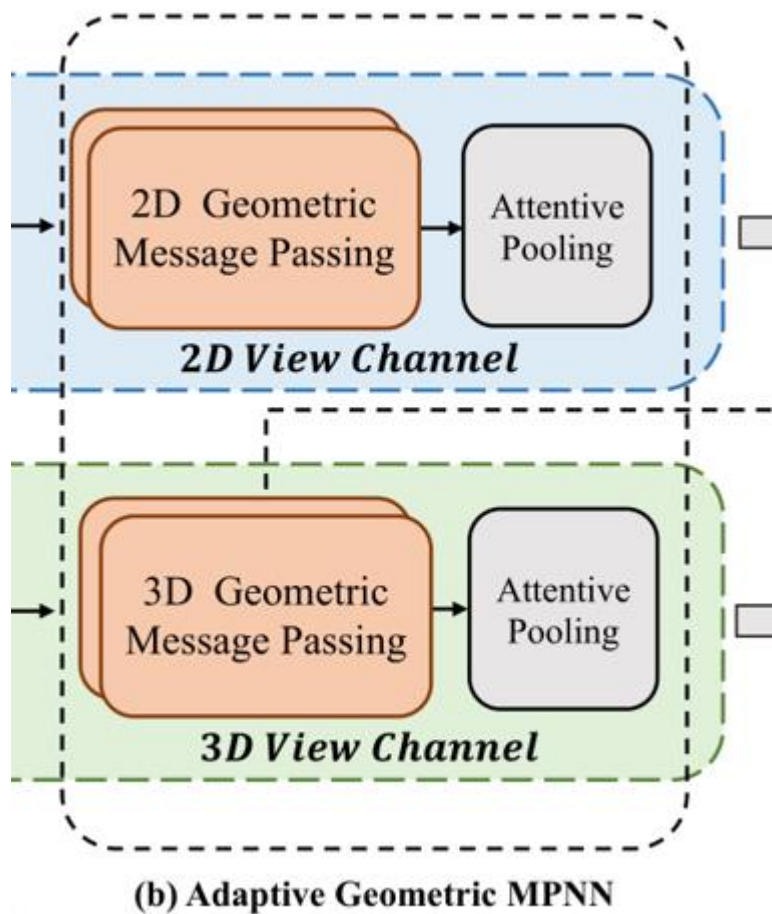
$$e_{uv}^{2d,t} = \sum_{e_{wu} \in \mathcal{A}(e_{uv})} W_{\phi}^t \phi_{wuv} \odot (W_e^t e_{uv}^{2d,t}) \quad (7)$$

$$e_{uv,i}^{3d,t} = \sum_{e_{wu} \in \mathcal{A}_i(e_{uv})} W_{\theta,i}^t \theta_{wuv} \odot (W_{e,i}^t e_{uv}^{3d,t}) \quad (8)$$

$$e_{uv}^{3d,t} = \bigparallel_{i=1}^n \text{Pool}(\{e_{uv,i}^{3d,t} \mid 1 \leq i \leq n\}) \odot e_{uv,i}^{3d,t} \quad (9)$$



# Method



## Edge $\rightarrow$ Node Message Passing

$$\mathbf{a}_v^{2d,t} = \sum_{e_{uv} \in \mathcal{D}(a_v)} W_l^t \mathbf{l}_{uv} \odot (W_a^t \mathbf{e}_{uv}^{2d,t}) \quad (10)$$

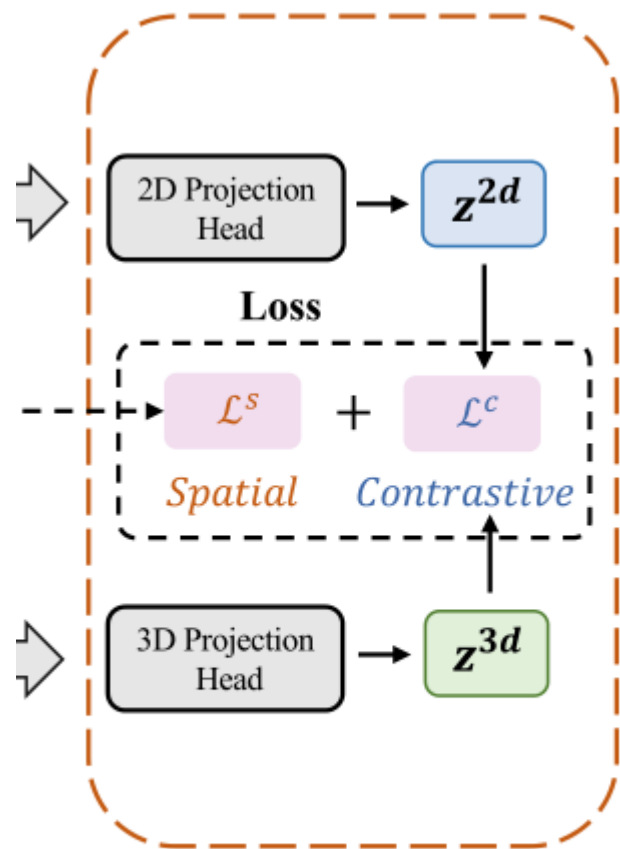
$$\mathbf{a}_v^{3d,t} = \parallel_{i=1}^m \sum_{e_{uv} \in \mathcal{D}_i(a_v)} W_{r,i}^t \mathbf{r}_{uv} \odot (W_{a,i}^t \mathbf{e}_{uv}^{3d,t}) \quad (11)$$

## Node $\rightarrow$ Graph Attentive Pooling

$$\mathbf{g}^t = \sum_{a_v \in \mathcal{V}} \text{softmax}(\mathbf{h}^t \parallel \mathbf{a}_v) W_g^t \mathbf{a}_v \quad (12)$$

$$\mathbf{h}^{t+1} = \text{GRU}(\mathbf{h}^t, \mathbf{g}^t), \quad t = 0, 1, \dots, T_g \quad (13)$$

# Method



(c) Geometric Graph Contrastive

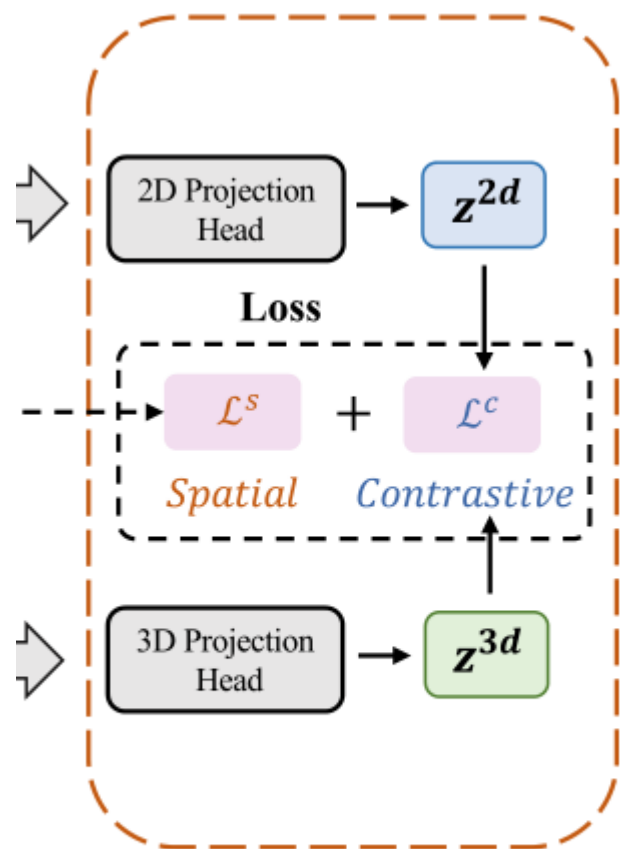
$$z_i^{2d} = MLP(h_i^{2d}), \quad z_i^{3d} = MLP(h_i^{3d}) \quad (14)$$

$$\begin{aligned} \mathcal{L}_i^c &= \mathcal{L}_i^{2d,c} + \mathcal{L}_i^{3d,c} \\ &= -\log \frac{e^{\langle z_i^{2d}, z_i^{3d} \rangle / \tau}}{\sum_{j=1}^N e^{\langle z_i^{2d}, z_j^{3d} \rangle / \tau}} - \log \frac{e^{\langle z_i^{3d}, z_i^{2d} \rangle / \tau}}{\sum_{j=1}^N e^{\langle z_i^{3d}, z_j^{2d} \rangle / \tau}} \end{aligned} \quad (15)$$

$$\mathcal{L}^s = \sum_{t=1}^T \sum_{i=1}^{n-1} \|W_{\theta, i+1}^t - W_{\theta, i}^t\|^2 \quad (16)$$



# Method



(c) Geometric Graph Contrastive

$$\hat{y} = MLP\left(MLP(f_{2d}(\mathcal{G}^{2d})) + MLP(f_{3d}(\mathcal{G}^{3d}))\right) \quad (18)$$

$$\mathcal{L}_{cls} = \mathcal{L}_{ce}(\hat{y}, y) + \lambda \mathcal{L}^s \quad (19)$$

$$\mathcal{L}_{reg} = \mathcal{L}_1(\hat{y}, y) + \lambda \mathcal{L}^s \quad (20)$$



# Experiment

Dataset	# Tasks	Task Type	# Molecules
ClinTox	2	Classification	1484
Sider	27	Classification	1427
Tox21	12	Classification	7831
ToxCast	617	Classification	8597
ESOL	1	Regression	1128
FreeSolv	1	Regression	643
Lipophilicity	1	Regression	4200

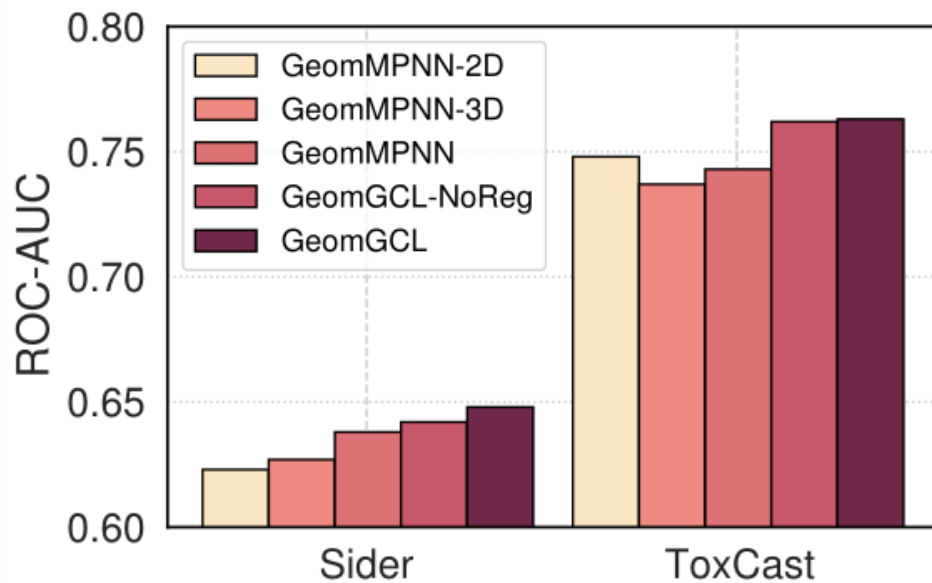
Table 1: Statistics of seven molecular datasets.



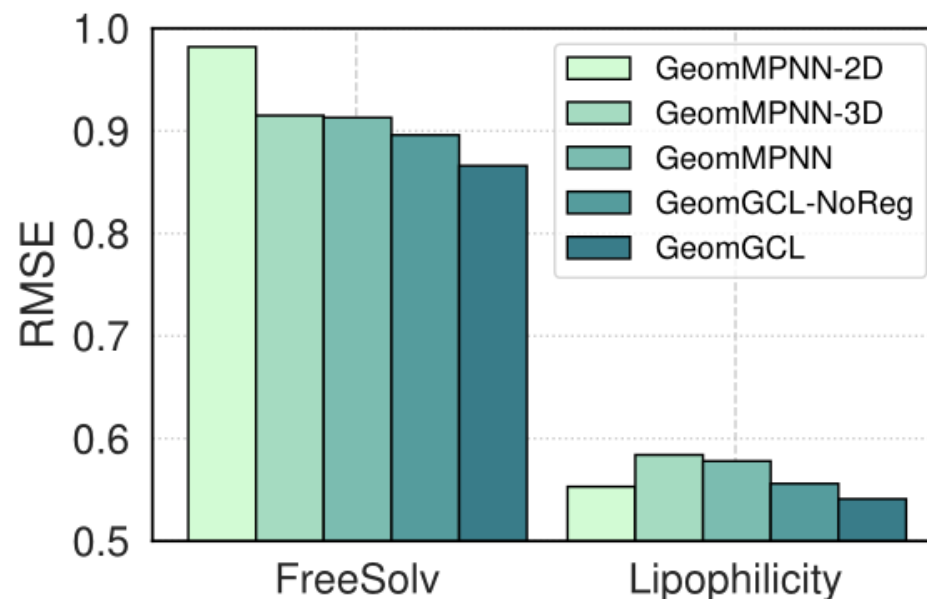
# Experiment

Model	Graph Classification (ROC-AUC) $\uparrow$					Graph Regression (RMSE) $\downarrow$			
	ClinTox	Sider	Tox21	ToxCast	Cls.Ave	ESOL	FreeSolv	Lipophilicity	Reg.Ave
AttentiveFP	0.808	0.605	0.835	0.743	0.748	0.578	1.034	0.602	0.738
DMPNN	0.886	0.637	0.848	0.743	0.779	0.647	1.092	0.591	0.777
CoMPT	0.877	0.626	0.836	0.755	0.774	0.589	1.103	0.590	0.761
SGCN	0.825	0.560	0.769	0.656	0.703	1.329	2.061	1.075	1.488
MAT	0.898	0.619	0.834	0.735	0.772	0.624	1.059	0.705	0.796
HMGNN	0.680	0.607	0.794	0.702	0.696	0.701	1.207	0.720	0.876
DimeNet	0.760	0.615	0.780	0.645	0.7000	0.633	0.978	0.614	0.742
InfoGraph	0.781	0.585	0.793	0.705	0.716	0.914	2.104	0.845	1.288
MoCL	0.739	0.629	0.824	0.718	0.727	0.934	1.478	0.742	1.051
GeomMPNN	0.900	0.638	0.838	0.743	0.780	<b>0.555</b>	0.913	0.578	0.682
GeomGCL	<b>0.919</b>	<b>0.648</b>	<b>0.850</b>	<b>0.763</b>	<b>0.796</b>	0.575	<b>0.866</b>	<b>0.541</b>	<b>0.661</b>

# Experiment



(a) Results for Classification



(b) Results for Regression

Figure 4: Evaluation of GeomGCL with its variants.

# Experiment

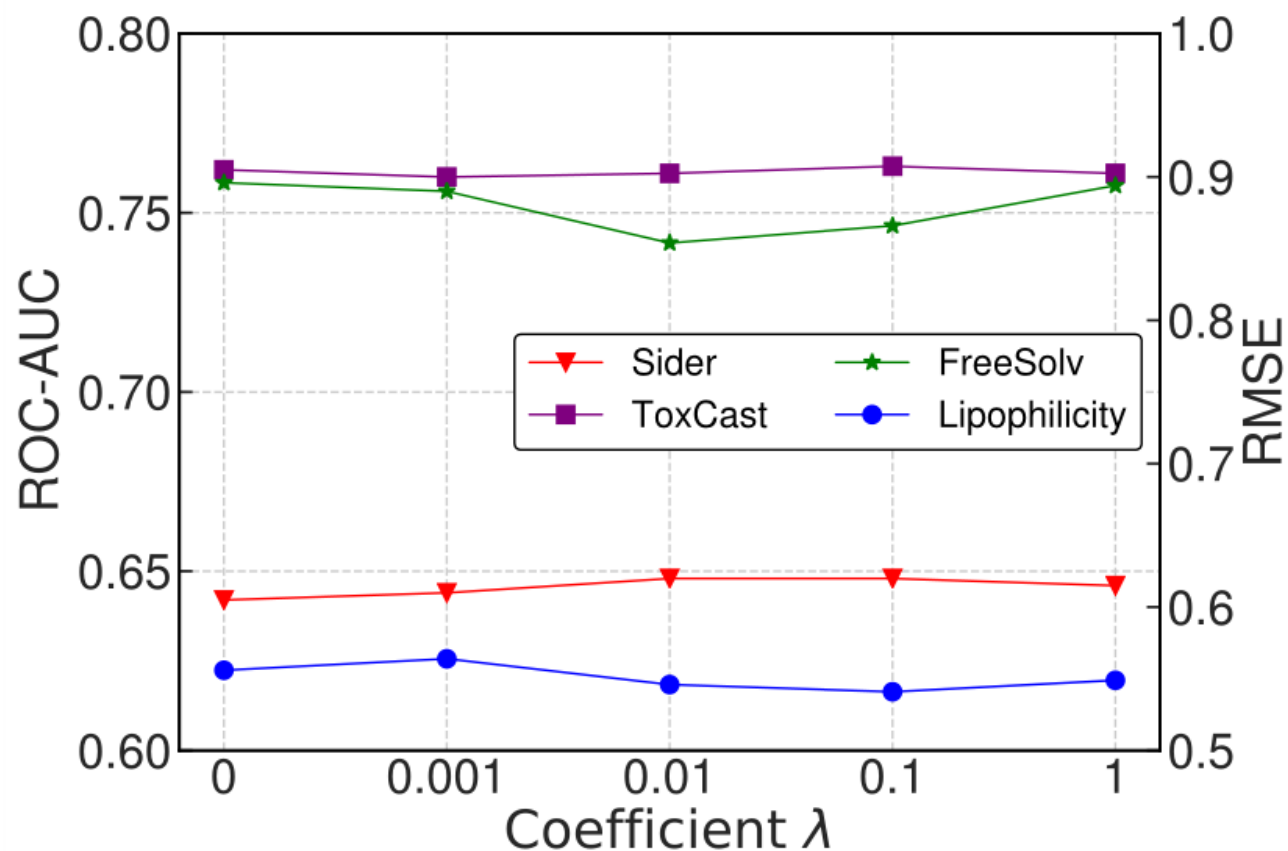


Figure 5: Analysis for the balancing parameter of  $\mathcal{L}^s$



# Thank you!

